

# Tools for Personalized Search

Devdatt Dubhashi  
Department of Computer Science and Engineering  
Chalmers University  
Gothenburg, Sweden.

The Future of Web Search, Bertinoro, June 17–20, 2007

# Outline

- 1 Introduction: Personalization Techniques
- 2 Ranking via Flows
- 3 co-Clustering

# Outline

- 1 Introduction: Personalization Techniques
- 2 Ranking via Flows
- 3 co-Clustering

# Outline

- 1 Introduction: Personalization Techniques
- 2 Ranking via Flows
- 3 co-Clustering

# Outline

- 1 Introduction: Personalization Techniques
- 2 Ranking via Flows
- 3 co-Clustering

# Review of Pagerank

- $\mathbf{C} := \alpha \mathbf{P} + (1 - \alpha) \frac{\mathbf{1}}{N}$ .
- Uniform random surfer model.

# Personalizing Pagerank: Teleport vector

- $\mathbf{C} := \alpha\mathbf{P} + (1 - \alpha)\mathbf{v}$ .
- Personalization vector  $\mathbf{v}$ .

# Outline

- 1 Introduction: Personalization Techniques
- 2 Ranking via Flows**
- 3 co-Clustering



# Network flow based ranking

- Given a directed graph  $G = (V, E)$ , a **flow**

$$f : E \rightarrow \mathbf{R},$$

defines a ranking on the nodes.

- The rank of a node  $v \in V$  with respect to the flow  $f$  is the **inflow**

$$f(v) := \sum_{(u,v) \in E} f(u, v).$$

- Very general framework: the graph  $G$  can be the Web (with teleport node etc.) or a biological network (gene interactions) or a semantic entity-relationship graph, [1]

# Example: Pagerank as Flow

- Given the transition matrix  $P$  of a reversible Markov chain, with the stationary distribution  $\pi$ , let

$$f(u, v) := \pi_u P(u, v).$$

- The ranking defined by this flow is exactly  $\pi$ :

$$\begin{aligned} f(v) &= \sum_u \pi_u P(u, v) \\ &= \sum_u \pi_v P(v, u) \\ &= \pi_v. \end{aligned}$$

# Incorporating User Preferences

- Users are allowed to express **preferences** in the form:

$$u \prec v.$$

- Such preferences could be collected via clickthrough data (Joachims 05, 07).
- Given a set of such preferences  $\mathcal{P}$ , can they be incorporated into the ranking?
- **Goal:** Find a ranking which is as “close” to pagerank as possible, and also **respects user preferences**  $\mathcal{P}$ .

# User Preferences: Convex Optimization

Chakrabarti *et al* [2] following others:

- Minimize the **Kullback-Liebler Divergence**

$$\min D(f||q) = \sum_{(u,v)} f(u,v) \log \frac{f(u,v)}{q(u,v)}$$

- with respect to the **reference flow**  $q$  say Pagerank,
- Subject to user preferences:

$$\sum_{(w,u) \in E} f(w,u) \leq \sum_{(w,v) \in E} f(w,v), \quad (u \prec v) \in \mathcal{P}.$$

# Acceleration: Incremental Computation

- Rather than solving the program from scratch, update solution to reflect new preferences.
- Compute a sequence  $f_0, f_1, \dots$  where
- $f_0$  is the **reference flow** (Pagerank)
- $f_{i+1}$  is computed by **updating**  $f_i$  to reflect a new preference  $u \prec v$ .
- Intuitively,  $f_{i+1}$  will be a “small” perturbation of  $f_i$  and hence can be computed fast.
- We use the fact that  $f_i$  is still **dual feasible**.

# Acceleration: Local Computation

- Also  $f_{i+1}$  is likely to differ from  $f_i$  only **locally** in a neighbourhood of the newly expressed preference  $u \prec v$ .
- Hence we may hope to compute  $f_{i+1}$  from  $f_i$  by a local update on a small subgraph  $H$  around  $u$  and  $v$ .
- If  $H$  is much smaller than the whole graph, this results in significant savings.
- Corresponding to a new preference  $u \prec v$ ,  $H$  will include the connected components of  $u$  and  $v$  in  $\mathcal{P}$ .
- Fix the flows between  $H$  and  $G \setminus H$  (constraints) and solve optimization problem on  $H$ .

# Outline

- 1 Introduction: Personalization Techniques
- 2 Ranking via Flows
- 3 co-Clustering**

# Co-clustering

- **Co-clustering** is simultaneous clustering of objects in different categories [3]
- $G := (V_1, V_2, \dots, V_k, E)$  a multi-partite graph corresponding to  $k$  different categories. (The edge set  $E$  may also include intra-class edges.)
- Example: People versus Movies, with  $k = 2$ .
- A co-clustering is a simultaneous clustering within each of the classes  $V_1, \dots, V_k$ .
- Different from separate clusterings in every class.
- A good clustering in one class can help clustering in the other classes via the relations in  $E$ : serves as a kind of **dimensionality reduction**.



# Application: Collaborative Filtering

- Users rate some movies.
- Based on these ratings, we can predict ratings for other movies.
- Windghager, Tansini *et al* apply it to data from the Hungarian web.

# Application: Mining User Intent from Weblogs

- **Users** enter
- **Queries** which retrieve
- **Documents**
- Co-clustering can help detecting **user intent**.
- Tansini applies it to **TodoCI** data.

# Agglomerative Iterative co-Clustering

- Label each object according to its link structure to classes in the other categories.
- Apply an agglomerative clustering technique based on this representation.
- Iterate. In each iteration, the representation of an object is different corresponding to the current clustering in the other classes.





# Information-theoretic co-clustering

- Dhillon *et al* [4] give an information–theoretic criterion for co–clustering.
- Maximize the **mutual information** between random variables corresponding to the clusterings in different classes.
- Results in a convex optimization problem.
- Local gradient approaches.
- Randomized rounding approaches.

# Semi-supervised Transductive Approaches

- Typically, labels on some objects may be known.
- Treat co-clustering as a **semi-supervised** or **transductive** learning problem.
- **Conditional Random Fields.**
- **Label Propagation via Graph Laplacians.**
- **Geometric regularization ...**

# For Further Reading I

-  [J.A. Tomlin](#)  
“A New Paradigm for Ranking pages on the World Wide Web”. WWW’03, 2003.
-  [A. Agrawal, S. Chakrabarti and S. Aggarwal](#)  
“Learning to Rank Networked Entities”, KDD’06, 2006
-  [A. Tanay, R. Sharan and R. Shamir](#)  
“Biclustering Algorithms: A Survey” in *Handbook of Computational Molecular Biology*, S. Aluru, editor, pp. 26-1 - 26-17, Chapman and Hall / CRC Press 2006
-  [I. S. Dhillon, S. Mallela, and D. S. Modha](#)  
“Information-Theoretic Co-clustering” KDD’03, 2003